

# Online State and Dynamic Parameter Estimation in Biotherapeutic Production through Ensemble Kalman Filtering

19th international EnKF workshop (2024)

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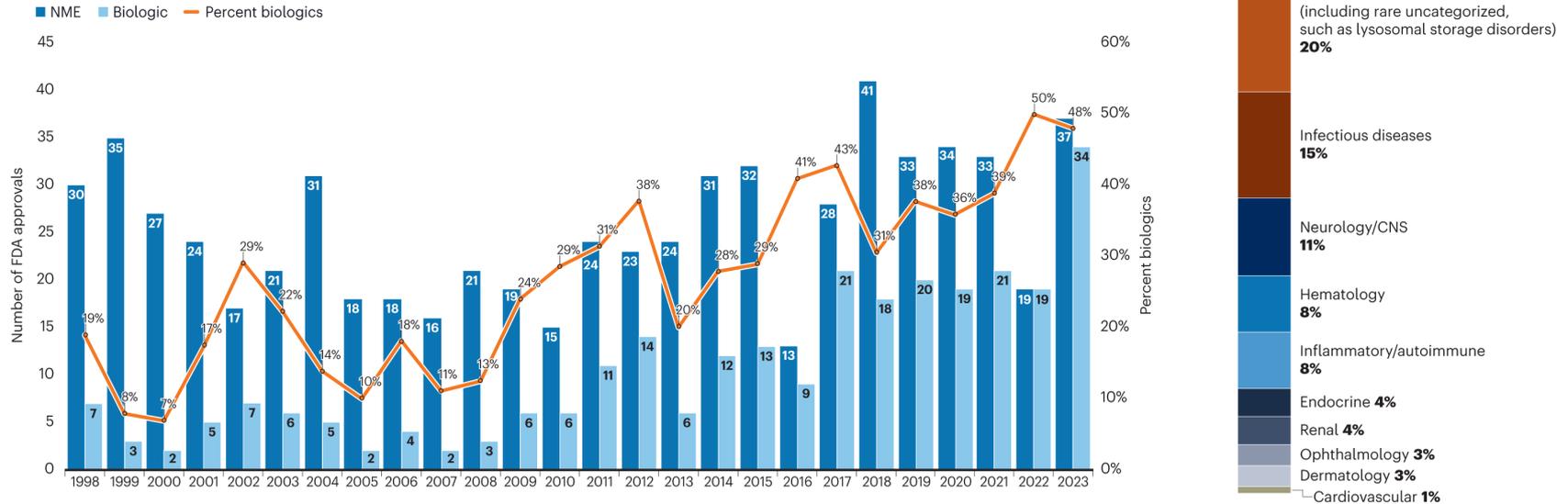
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## Overview

- Introduction of biotherapeutics and bioprocessing
- Applying mathematical modelling and challenges
- Motivation for employing EnKF for  
**Combined State and Parameter Estimation**
- Case Study: Applying EnKF for  
**Online State and Dynamic Parameter Estimation of a Mild Hypothermia Process**
- **Please help-challenges ahead**

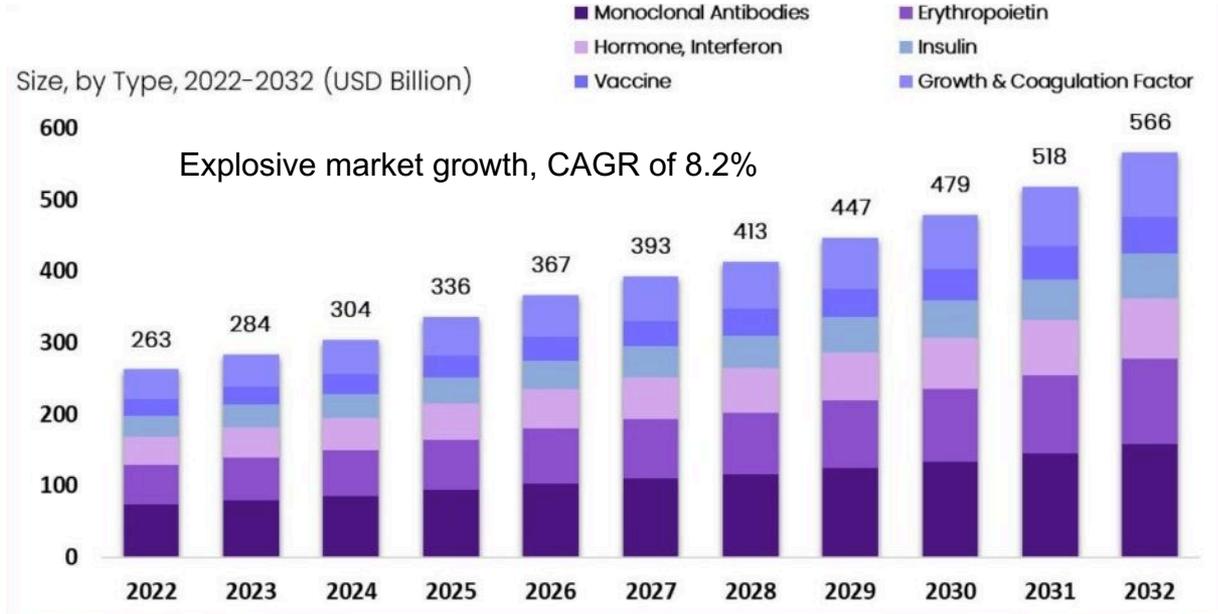
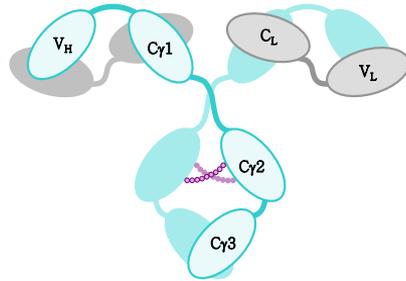
# Biologics: Record-breaking FDA approvals

## Biologically derived drugs



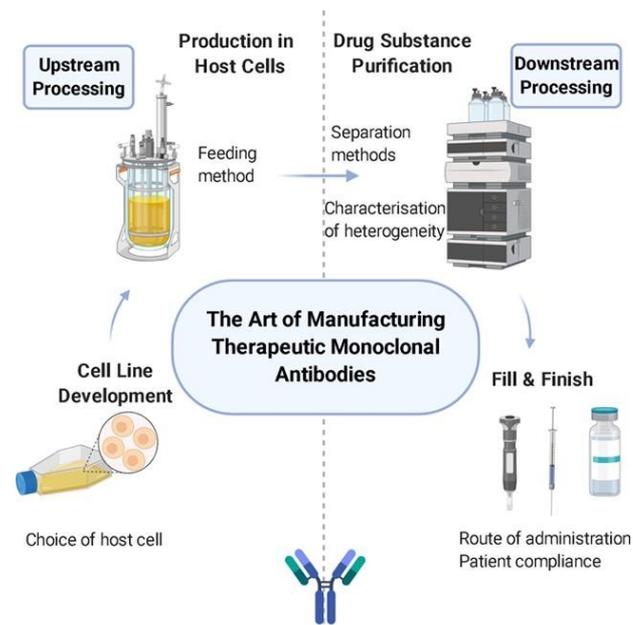
# Global Biopharmaceuticals Market

- Dominated by **Monoclonal Antibodies (mAb)**
- Highly specific targeting

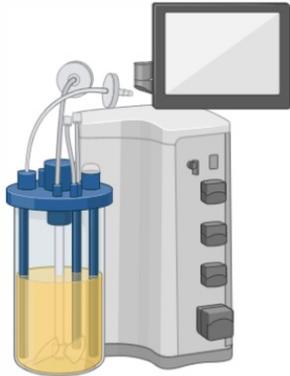


## Bioprocessing of therapeutic proteins in mammalian cells

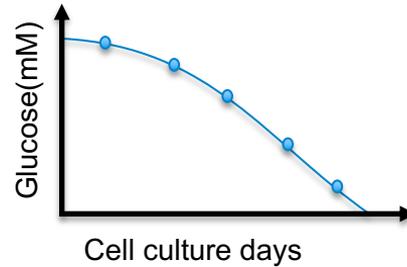
- Industrial production of therapeutic proteins, rely on living cells
- Mammalian cells are favoured due to compatibility to human bodies
- Nearly 70% of therapeutic proteins are produced in Chinese Hamster Ovary (CHO) cells.



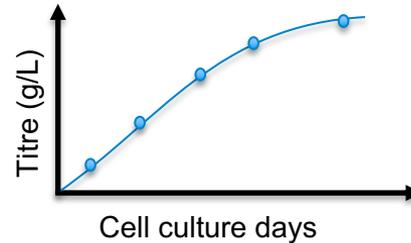
## Mechanistic model development



Data Collection



Model Development



$$\mu = \mu_{max} \prod_{i=1}^{N.C.} \left( \frac{C_i}{K_{M,i} + C_i} \right)$$

$$q_i = \alpha_i \left( \frac{C_i}{K_{M,i} + C_i} \right)$$

$$q_p = \alpha_p \sum_{i=1}^{N.C.} \alpha_i q_i$$

**Monod Kinetics**

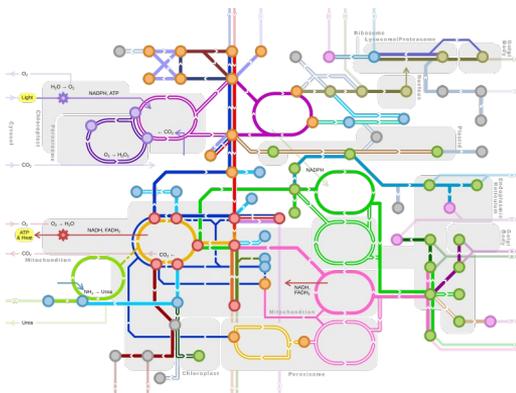
$$\frac{d(VX_V)}{dt} = \mu VX_V - Q_{out}X_V$$

$$\frac{d(VC_{i,in})}{dt} = Q_{in}C_{i,in} - Q_{out}C_i + q_i VX_V$$

$$\frac{d(VP)}{dt} = q_p VX_V - Q_{out}P$$

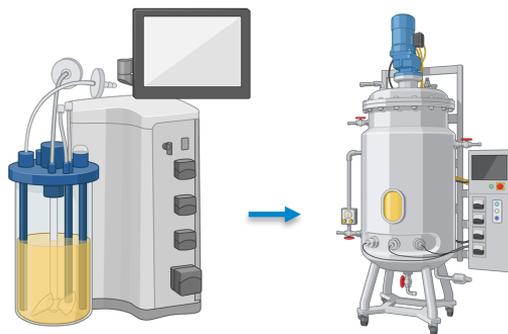
**Material Balances**

## Challenges in applying mechanistic models



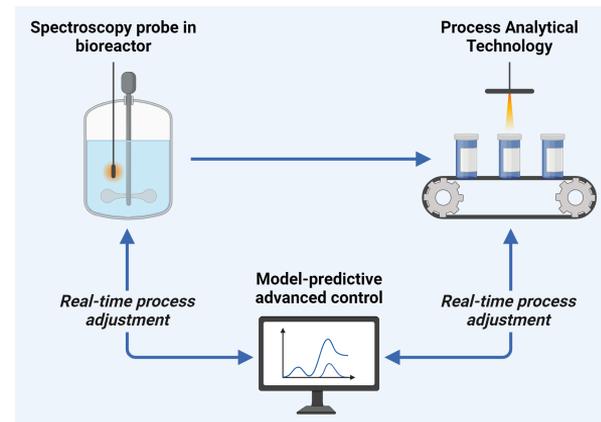
Complexity of biological systems:

- non-linear system dynamics
- parameter sensitivity and identifiability
- Inherent variability but fixed parameter



Challenges in knowledge transfer:

- specific to cell line, experimental condition and scale
- high quality and comprehensive data required for validation



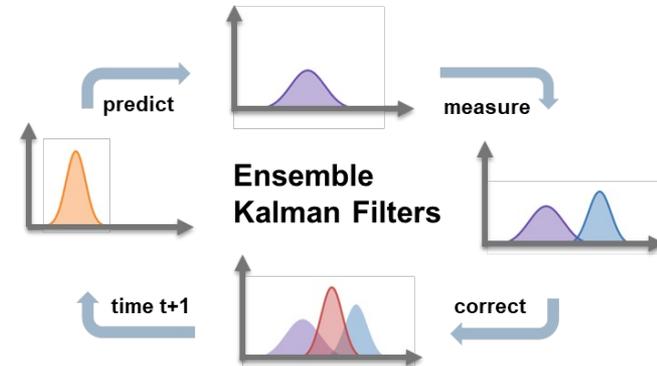
Integration with process control:

- require models to be adaptable and responsive to real-time data
- models need to be robust to deal with uncertainty and variability

## Motivation for applying Ensemble Kalman Filter (EnKF)

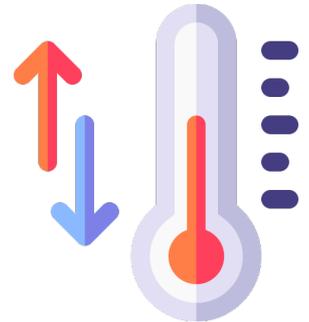
### Ideally...

- Avoid reparametrize the model from scratch for a different system
- Identify uncertainty explicitly:
  - Fundamental differences – e.g. different cell lines/metabolic pathways
  - Does it come from biological variability?- e.g. same cell line
  - Does it come from sensor noise? Parameters? Inputs? Outputs?
- Knowledge transfer – parameters that needs to be adjusted/kept same
- Robust model for online real time control, allow dynamic adaptation of states and parameters



## Case Study: Temperature Downshifts in Bioprocessing

- Mild hypothermia: temperature downshift half-way through the production run
- Common practice in industry to enhance cell culture productivity
- Slow down cell growth/death, higher viability of cells, higher titre and less impurities
- Challenge:
  - highly specific mechanistic model, no temperature dependence understanding
  - time invariant parameters unsuitable for flexible temperature downshift regime

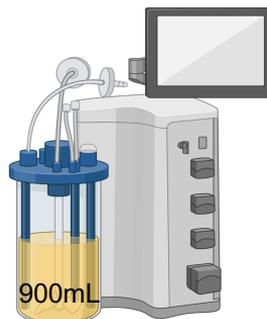


## Case Study: Temperature Downshifts in Bioprocessing



Shake flask

- Cell-line: CHO-T127
- Product: IgG
- Fed-batch (feed every 2 days)
- Volume: 100mL
- No pH, antifoam control
- Temperature: 36.5 °C
- Model: (Kotidis *et al.* 2019)



Bioreactor

- Cell-line: CHO-T127
- Product: IgG
- Fed-batch (feed every 2 days)
- Volume: 900mL
- pH, antifoam control
- Day 6 temperature downshift: 32 °C

EnKF Combined States and Parameter Estimation  
(True: Sou *et al.* 2017 32 °C)

No. of states: 8; No. of parameters: 24

## EnKF for dual state and parameter estimation-algorithm

- Parameter evolution, sample parameters
- State ensemble prediction with sampled parameters

$$\theta_{t+1}^{i-} = \theta_t^{i+} + \tau_t^i, \quad \tau_t^i \sim N(0, \Sigma_t^\theta)$$

$$x_{t+1}^{i-} = f(x_t^{i+}, u_t^i, \theta_{t+1}^{i-})$$

- Update parameter ensemble members according to standard EnKF

$$\theta_{t+1}^{i+} = \theta_{t+1}^{i-} + K_{t+1}^\theta (y_{t+1}^i - \hat{y}_{t+1}^i)$$

where Kalman gain for parameters is

$$K_{t+1}^\theta = \Sigma_{t+1}^{\theta y} [\Sigma_{t+1}^{yy} + \Sigma_{t+1}^y]^{-1}$$

$i$  : Ensemble member  
 $i^-$  : Forecasted  
 $i^+$  : Updated  
 $\theta$  : Model parameters  
 $y$  : Process measurements  
 $x$  : Process states  
 $K$  : Kalman gain

**EnKF for parameter estimation**

- State ensemble prediction with updated parameters
- Update state ensemble members

$$x_{t+1}^{i-} = f(x_t^{i+}, u_t^i, \theta_{t+1}^{i+})$$

$$x_{t+1}^{i+} = x_{t+1}^{i-} + K_{t+1}^x (y_{t+1}^i - \hat{y}_{t+1}^i)$$

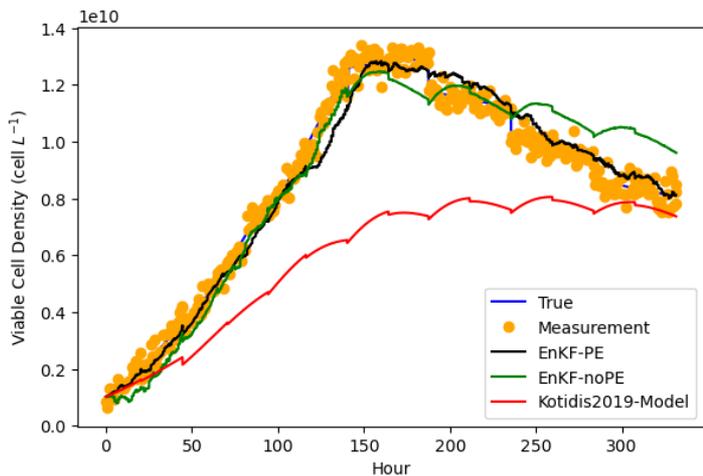
**Standard EnKF**

where Kalman gain matrix for state

$$K_{t+1}^x = \Sigma_{t+1}^{xy} [\Sigma_{t+1}^{yy} + \Sigma_{t+1}^y]^{-1}$$

## Cell growth and death

$$\frac{d(VX_v)}{dt} = (\mu - \mu_{death}) VX_v - F_{out} X_v$$

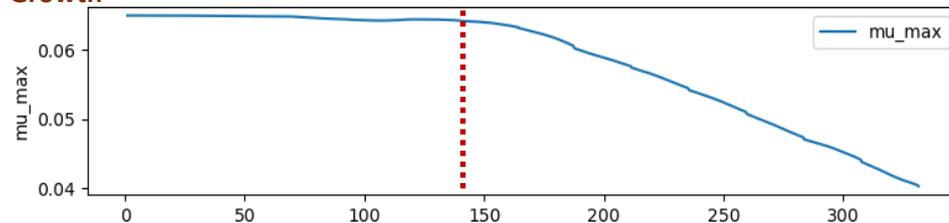


$$\mu = \mu_{max} f_{lim} f_{inh}$$

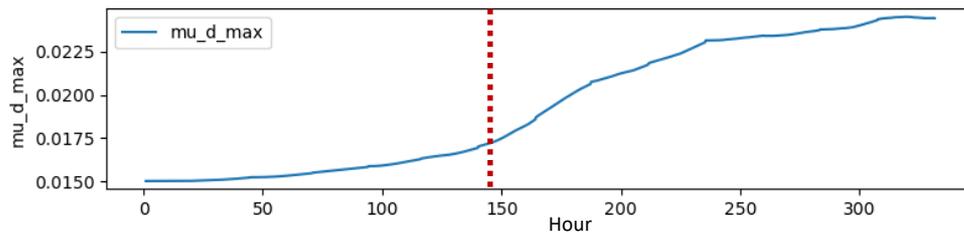
$$\mu_{death} = \mu_{death,max} \left( \frac{[Amm]}{[Amm] + K_{d,Amm}} + \frac{[Urd]}{[Urd] + K_{d,Urd}} \right)$$

Temperature  
Downshift

Growth



Death

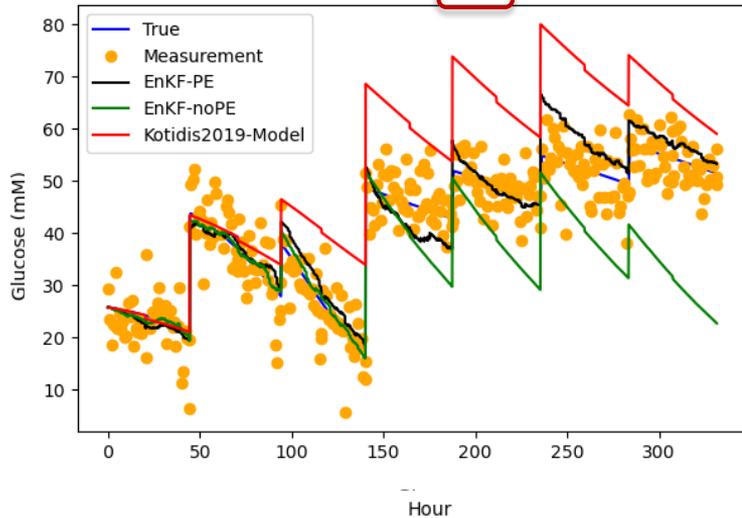


# Glucose: main nutrient for cell growth

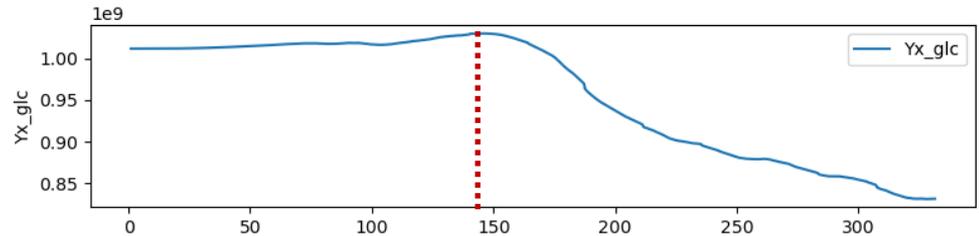
Temperature  
Downshift

$$\frac{d(V[\text{Metabolite}])}{dt} = F_{in}[\text{Metabolite}_{feed}] - F_{out}[\text{Metabolite}] + q_{Glc} V X_v$$

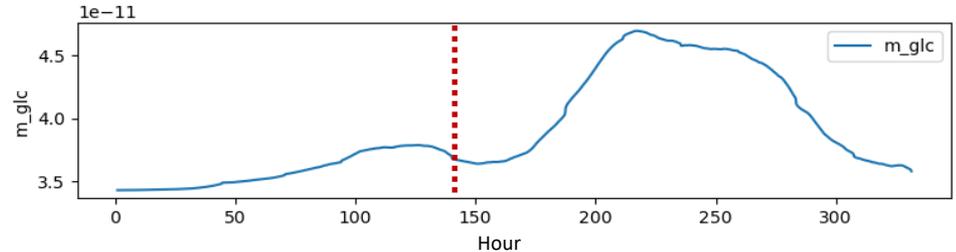
$$q_{Glc} = \left( -\frac{\mu}{Y_{X_{Glc}}} - m_{Glc} \right)$$



Yield of biomass from glucose



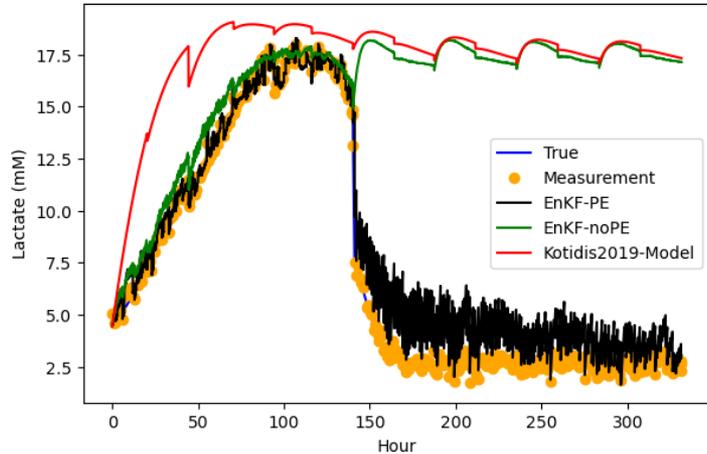
Consumption towards other pathways



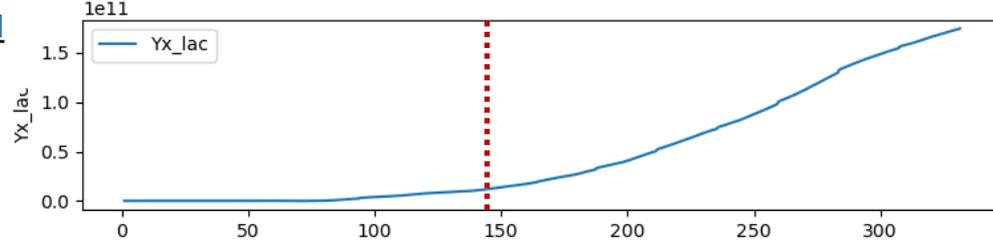
# Lactate: by product of glucose metabolism, contribute to cell death

$$\frac{d(V[\text{Metabolite}])}{dt} = F_{in}[\text{Metabolite}_{feed}] - F_{out}[\text{Metabolite}] + q_{Lac} V X_v$$

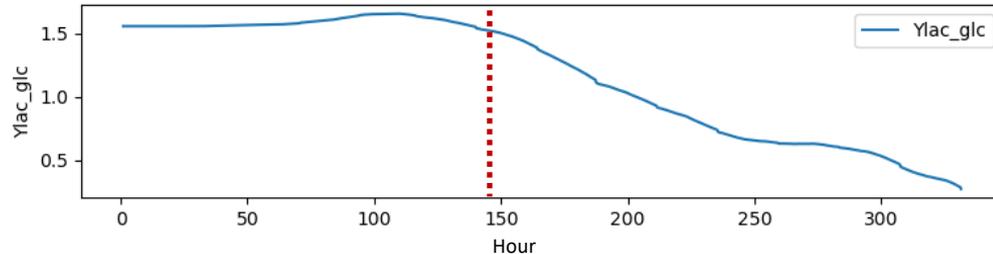
$$q_{Lac} = \left( \frac{\mu}{Y_{X_{Lac}}} - Y_{Lac/Glc} q_{Glc} \right) \frac{(Lac_{max1} - [Lac])}{La_{max1}} + m_{lac} \frac{La_{max2} - [Lac]}{La_{max2}}$$



Yield of biomass from lactate

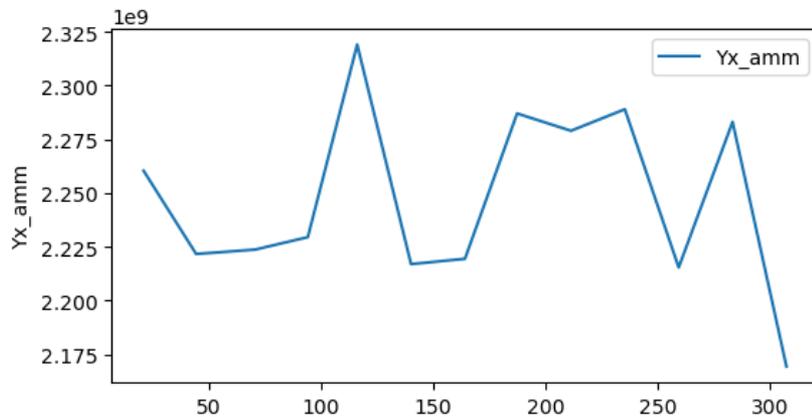
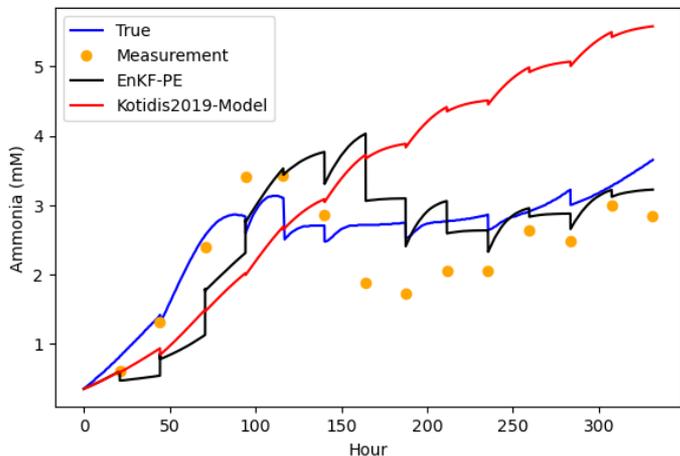


Yield of lactate from glucose



Temperature  
Downshift

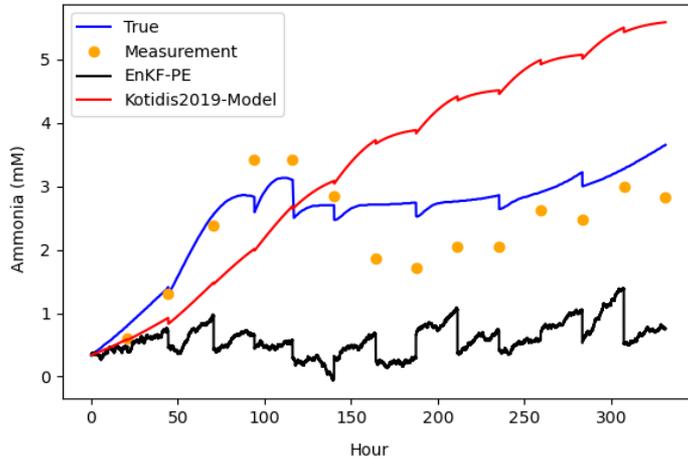
## Question 1: Real process data: sparse measurement



Made a mistake in code **but 'worked'** : at each step the current ensemble is discarded, new ensemble created based on current mean value

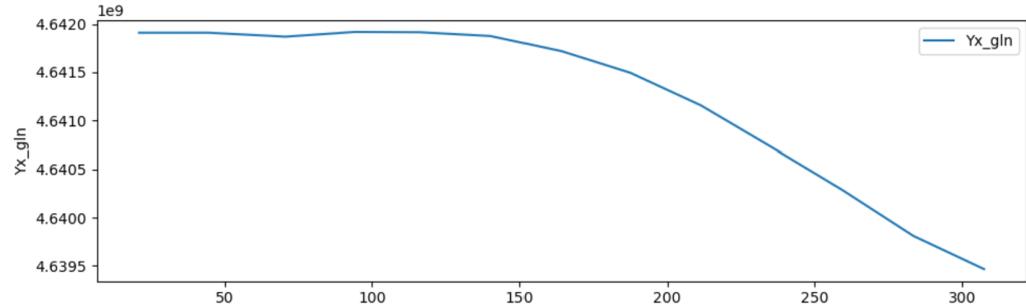
Is this parameter evolution purely based on noise?

## Question 1(continued): Real process data, sparse measurement



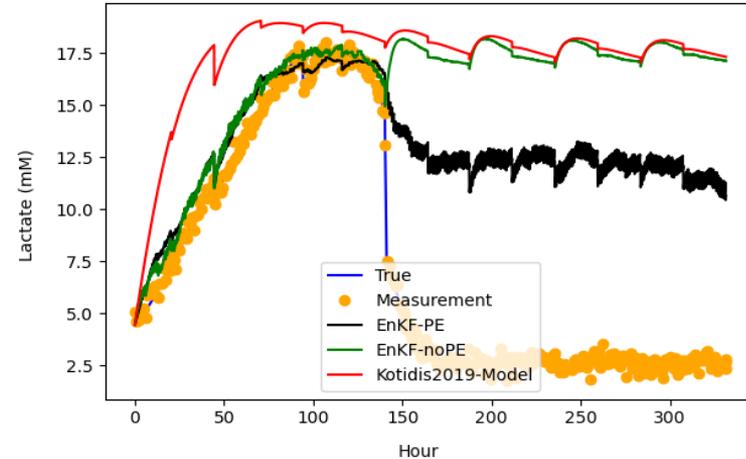
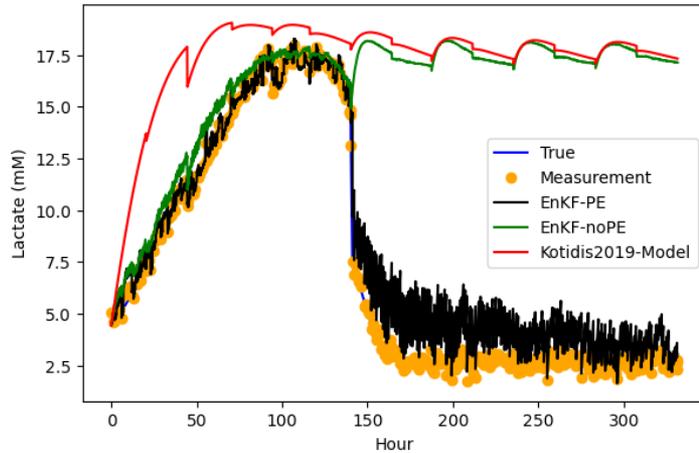
Propagate the ensemble of parameters:  
every ensemble member follow random  
walk, does not work.

- Is this a problem of tuning only?



- How to assess if PE is needed?
- If PE is not needed, can we use ensemble parameter estimation method for understanding the dynamic variation of system? –parameter no longer fixed
- How to overcome limitation of sparse measurement?

## Question 2: For very different profile, how to smooth the curve when EnKF heavily depends on observations?



**Question 3: How to assess which parameters require reparameterization and a systematic way for tuning? At least a good starting point?**

**Thank you very much for the help!**

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